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Mathematics 5B Spring 2011: Lecture Quiz 2

April 15, 2011

Professor J. Douglas Moore

Multiple Choice. Circle the best answer to each of the following questions. Each question is worth 2 points.

1. A parametrization of the line segment in \mathbb{R}^3 from $(1, 3, 2)$ to $(4, 4, 5)$ is the map $\mathbf{x} : [0, 1] \rightarrow \mathbb{R}^3$ such that

a. $\mathbf{x}(t) = (1+t) \begin{pmatrix} 1 \\ 3 \\ 2 \end{pmatrix} + t \begin{pmatrix} 3 \\ 1 \\ 3 \end{pmatrix}$

b. $\mathbf{x}(t) = (1+t) \begin{pmatrix} 1 \\ 3 \\ 2 \end{pmatrix} + t \begin{pmatrix} 4 \\ 4 \\ 5 \end{pmatrix}$

c. $\mathbf{x}(t) = (1-t) \begin{pmatrix} 1 \\ 3 \\ 2 \end{pmatrix} + t \begin{pmatrix} 3 \\ 1 \\ 3 \end{pmatrix}$

d. $\mathbf{x}(t) = (1-t) \begin{pmatrix} 1 \\ 3 \\ 2 \end{pmatrix} + t \begin{pmatrix} 4 \\ 4 \\ 5 \end{pmatrix}$

e. None of these

2. If a curve C is parametrized in polar coordinates by $r = r(t)$ and $\theta = \theta(t)$, where $a \leq t \leq b$, then it follows from the chain rule that its length in the (x, y) -plane is given by the formula

$$L(C) = \int_a^b \sqrt{\left(\frac{dr}{dt}\right)^2 + r^2 \left(\frac{d\theta}{dt}\right)^2} dt.$$

Consider the curve C parametrized by $r = e^{-t}$, $\theta = t$, for $0 \leq t \leq 2\pi$. The length of this curve in the (x, y) -plane is

a. $1 - e^{-2\pi}$

b. $1 + e^{-2\pi}$

c. $\sqrt{2}(1 - e^{-2\pi})$

d. $\sqrt{2}(1 + e^{-2\pi})$

e. None of these

$$= \int_0^{2\pi} \sqrt{2e^{-2t}} dt = \int_0^{2\pi} \sqrt{2} e^{-t} dt$$

$$= \sqrt{2} (e^{-t}) \Big|_0^{2\pi} = \sqrt{2} (1 - e^{-2\pi})$$