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3) $f: x \to 5x+7 \pmod{26}$

h	o	w	a	r	e	y	o	u
7	14	22	0	17	4	24	14	20

h) $5(7)+7 = 42 \equiv 16 \pmod{26} \to Q$
o) $5(14)+7 = 77 \equiv 25 \pmod{26} \to Z$
w) $5(22)+7 = 117 \equiv 13 \pmod{26} \to N$
a) $5(0)+7 = 7 \quad (\sim) \to H$
r) $5(17)+7 = 92 \equiv 14 \quad (\sim) \to O$
e) $5(4)+7 = 27 \equiv 1 \quad (\sim) \to B$
y) $5(24)+7 = 127 \equiv 23 \quad (\sim) \to X$
o) $5(14)+7 \equiv 25 \quad (\sim) \to Z$
u) $5(20)+7 \equiv 3 \quad (\sim) \to D$

Ciphertext: Q Z N H O B X Z D

since $\gcd(5, 26) = 1$ then inverse exist
so $5x \equiv 1 \pmod{26}$
$x = 21$
$\to 5(21) = 105 \equiv 1 \pmod{26}$

Decryption (in) $5x+7 \equiv y \pmod{26}$
$21(5)x + 21(7) \equiv 21y \quad (\sim)$
$\to x + 147 \equiv 21y \quad (\sim)$
$x \equiv 21y - 147 \equiv 21y - 17 \pmod{26}$

Check $21(13) - 17 = 256 \equiv 22 \pmod{26}$ $f^{-1}: 13 \to 22$ ✓
~~$21(19) - 17 = 487 \equiv 19 \pmod{26}$ f~~
$21(23) - 17 = 466 \equiv 24 \pmod{26}$ $f^{-1}: 23 \to 24$ ✓