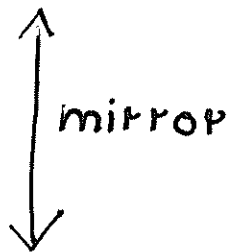


(a)

$$\mathcal{I}(+) = \frac{t}{2} \pm \dots$$

$L_+ - L_-$: trivial in $Fuk(X)$



trivial in $D^b(\text{Coh } Y)$

(Branes on Fermat quintic X)



(Branes on Fermat mirror quintic Y)

matrix factorizations

$$\left(\sum x_i^5 - 5 \psi \prod x_i \right) I_n = (\text{poly ent.}) (\text{poly ent.})$$

mirror of $L_+ - L_- = \mathcal{L}$ elt of $D^b(\text{Coh } Y)$
(8 terms cplx, rather messy)

$ch(\mathcal{L}) = 0$ in K -theory
 $ch^{alg}(\mathcal{L}) \neq 0$ represent. by $C_+ - C_-$
 C_{\pm} h.d. curves on Y

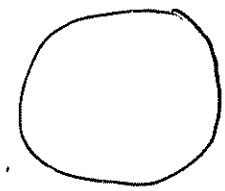
(b)

$$C_+ - C_- = \partial \Gamma \quad \Gamma = 3 \text{ char}$$

$\tilde{J}(z) = \int_{\Gamma} \Omega_z$ will descr. as elt of family of unterm. Jacobians over $\{z\}$

$$\partial_{\infty} \tilde{J}(z) = \int_{\Gamma} \Upsilon_z$$

$$\begin{aligned} H^3_{\mathbb{Z}} &\cong H^{3,0+2,1+1,2} \\ &\cong H^{3,0+2,1} \\ &\cong H^{3,0} \end{aligned}$$



$$(H^{3,0} + H^{2,1})^* \cong H_3(\cdot, \mathbb{Z})$$

$$\bar{C}_+, \bar{C}_- : (x_1^5 + x_2^5 + \dots + x_5^5 - 5\psi x_1 \dots x_5 = 0) / \mathbb{Z}_5^3$$

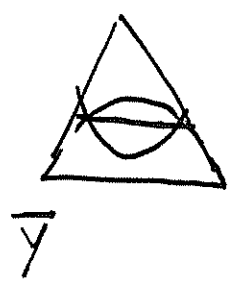
mirror of $L_+ - L_-$

$$x_1 + x_2 = x_3 + x_4 = 0 \quad (\text{a } \mathbb{C}P^2 \subseteq \mathbb{C}P^4)$$

$$0 = x_5^5 - 5\psi x_1^2 x_3^2 x_5$$

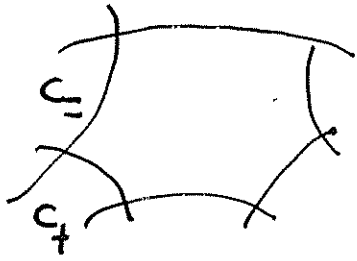
$$= x_5 \left(x_4^2 - \sqrt{5\psi} x_1 x_3 \right) \bar{C}_+ \\ \left(x_4^2 + \sqrt{5\psi} x_1 x_3 \right) \bar{C}_-$$

$$\bar{C}_+ - \bar{C}_- = \partial \bar{\Gamma}_3$$



lift (resolution)

(c)



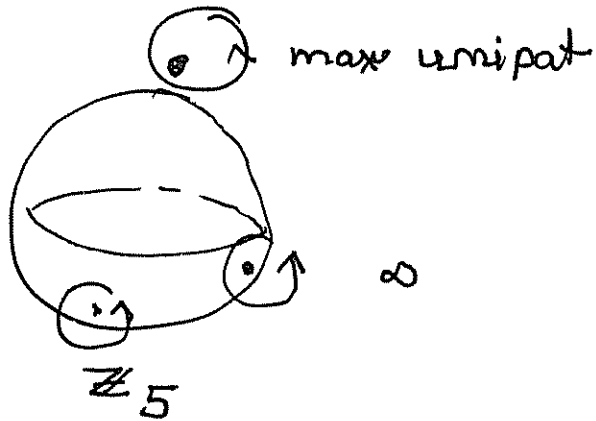
$$c_+ - c_- = \partial \Gamma_3$$

$$\psi. \Gamma_3 \subseteq \mathbb{C}P^2 \Rightarrow \int_{\Gamma_3} \Omega = 0$$

but you can't force $\Gamma_3 \subseteq \mathbb{C}P^2$;
only away from intersection pts.

$$\int_{\Gamma} \Omega_{\psi} = \frac{15}{16\pi^2} \sqrt{2}$$

monodromy



$$D' \int \Omega_z = 0$$

$$D \int \phi = 0 \Rightarrow D' \phi = 0$$

$$J(+)=$$