

Problem 3

A digraph G is said to be r -regular if each vertex in G has outdegree and indegree exactly r . The girth g of G is the length of a shortest cycle in G . Show that if G is a 3-regular digraph of order 7, then the girth g of G satisfies $g \leq \lceil 7/3 \rceil$.